

$$U(\mathbf{r}) = A \exp(-j\mathbf{k} \cdot \mathbf{r})$$

$$(\nabla^2 + k^2)U(\mathbf{r}) = 0$$

$$\nabla^2 u - \frac{1}{c^2} \frac{\partial^2 u}{\partial t^2} = 0$$

$$U(\mathbf{r}) = \frac{A}{r} \exp(-jkr)$$

$$k = \frac{2\pi\nu}{c} = \frac{\omega}{c}$$

$$U(\mathbf{r}, t) = U(\mathbf{r}) \exp(j2\pi\nu t)$$

$$U(\mathbf{r}) \approx \frac{A}{z} \exp(-jkz) \exp\left[-jk \frac{x^2 + y^2}{2z}\right]$$

$$U(\mathbf{r}) = A(\mathbf{r}) \exp(-jkz) \quad u(\mathbf{r}, t) = |A(\mathbf{r})| \cos[2\pi\nu t - kz + \arg\{A(\mathbf{r})\}]$$

$$\nabla_T^2 A - j2k \frac{\partial A}{\partial z} = 0$$

$$U(\mathbf{r}) = A_0 \frac{W_0}{W(z)} \exp\left[-\frac{\rho^2}{W^2(z)}\right] \exp\left[-jkz - jk \frac{\rho^2}{2R(z)} + j\zeta(z)\right]$$

$$U_{l,m}(x, y, z) = A_{l,m} \left[\frac{W_0}{W(z)} \right] \mathbb{G}_l \left[\frac{\sqrt{2}x}{W(z)} \right] \mathbb{G}_m \left[\frac{\sqrt{2}y}{W(z)} \right] \exp\left[-jkz - jk \frac{x^2 + y^2}{2R(z)} + j(l+m+1)\zeta(z)\right]$$

$$\mathbb{G}_l(u) = \mathbb{H}_l(u) \exp\left(\frac{-u^2}{2}\right), \quad l = 0, 1, 2, \dots$$

$$U_{l,m}(\rho, \varphi, z) = A_{l,m} \left[\frac{W_0}{W(z)} \right] \left(\frac{\rho}{W(z)} \right)^l L_m^l \left(\frac{2\rho^2}{W^2(z)} \right) \exp\left(-\frac{\rho^2}{W^2(z)}\right) \exp\left[-ikz - ik \frac{\rho^2}{2R(z)} - il\varphi + (l+2m+1)\zeta(z)\right]$$

$$U(\mathbf{r}) = A(x, y) e^{-j\beta z} \quad \nabla_T^2 A + k_T^2 A = 0 \quad k_T^2 + \beta^2 = k^2 \quad \nabla_T^2 = \partial^2 / \partial x^2 + \partial^2 / \partial y^2$$

$$A(x, y) = A_m J_m(k_T \rho) e^{jm\phi}, \quad m = 0, \pm 1, \pm 2$$